

$$i) \quad \Psi(x_1, x_2, x_3) = \Psi_a(x_1) \Psi_b(x_2) \Psi_c(x_3)$$

or

$$\Psi(x_1, x_2, x_3) = \Psi_b(x_1) \Psi_a(x_2) \Psi_c(x_3)$$

or any other similar product

ii)

$$\Psi(x_1, x_2, x_3) = \frac{1}{\sqrt{6}} \left[\Psi_a(x_1) \Psi_b(x_2) \Psi_c(x_3) + \Psi_b(x_1) \Psi_a(x_2) \Psi_c(x_3) + \Psi_b(x_1) \Psi_c(x_2) \Psi_a(x_3) + \Psi_c(x_1) \Psi_b(x_2) \Psi_a(x_3) + \Psi_c(x_1) \Psi_a(x_2) \Psi_b(x_3) + \Psi_a(x_1) \Psi_c(x_2) \Psi_b(x_3) \right]$$

The above expression includes all $6 = 3!$ permutations of particles. It is symmetric with respect to all permutations, and is normalized such that

$$\int |\Psi(x_1, x_2, x_3)|^2 dx_1 dx_2 dx_3 = 1$$

ii) The situation here is similar, except that even and odd permutations enter with different sign. This can be represented as a Slater determinant:

$$\Psi(x_1, x_2, x_3) = \frac{1}{\sqrt{6}} \begin{vmatrix} \Psi_a(x_1) & \Psi_a(x_2) & \Psi_a(x_3) \\ \Psi_b(x_1) & \Psi_b(x_2) & \Psi_b(x_3) \\ \Psi_c(x_1) & \Psi_c(x_2) & \Psi_c(x_3) \end{vmatrix} =$$

$$= \frac{1}{\sqrt{6}} \left[\Psi_a(x_1) \Psi_b(x_2) \Psi_c(x_3) - \Psi_b(x_1) \Psi_a(x_2) \Psi_c(x_3) + \Psi_b(x_1) \Psi_c(x_2) \Psi_a(x_3) - \Psi_c(x_1) \Psi_b(x_2) \Psi_a(x_3) + \Psi_c(x_1) \Psi_a(x_2) \Psi_b(x_3) - \Psi_a(x_1) \Psi_c(x_2) \Psi_b(x_3) \right]$$